

6.2

Lesson

Key Vocabulary

experimental probability, p. 475
 theoretical probability, p. 476
 simulation, p. 478

Key Idea

Experimental Probability

Probability that is based on repeated trials of an experiment is called **experimental probability**.

$$P(\text{event}) = \frac{\text{number of times the event occurs}}{\text{total number of trials}}$$

Example 1 Finding an Experimental Probability

Heads	Tails
6	19

The table shows the results of spinning a penny 25 times. What is the experimental probability of spinning heads?

Heads was spun 6 times in a total of $6 + 19 = 25$ spins.

$$P(\text{event}) = \frac{\text{number of times the event occurs}}{\text{total number of trials}}$$

Experimental probabilities are found the same way as relative frequencies.

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$$P(\text{heads}) = \frac{6}{25}$$

Heads was spun 6 times.

There was a total of 25 spins.

▶ The experimental probability is $\frac{6}{25}$, 0.24, or 24%.

Try It

The table shows the results of rolling a number cube 50 times. Find the experimental probability of the event.

Number Rolled	1	2	3	4	5	6
Frequency	10	4	8	11	11	6

how many times you rolled that #

1. rolling a 3

$$\frac{8}{50} = 0.16$$

16%

2. rolling an odd number

$$10 + 8 + 11 = 29$$

$$\frac{29}{50} = 0.58$$

58%



Key Idea

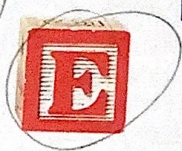
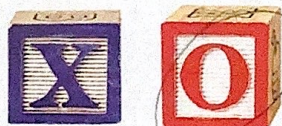
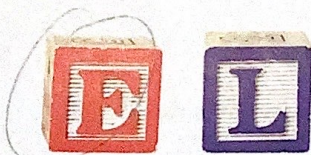
Theoretical Probability

When all possible outcomes are equally likely, the **theoretical probability** of an event is the quotient of the number of favorable outcomes and the number of possible outcomes.

$$P(\text{event}) = \frac{\text{number of favorable outcomes}}{\text{number of possible outcomes}}$$

Example 2 Finding a Theoretical Probability

You randomly choose one of the letters shown. What is the theoretical probability of choosing a vowel? A E I O U



$$P(\text{vowel}) = \frac{\text{number of favorable outcomes}}{\text{number of possible outcomes}} = \frac{3}{7}$$

There are 3 vowels.

There is a total of 7 letters

▶ The probability of choosing a vowel is $\frac{3}{7}$, or about 43%.

3 vowels

7 total letters

= 0.4285

about 43%

Try It

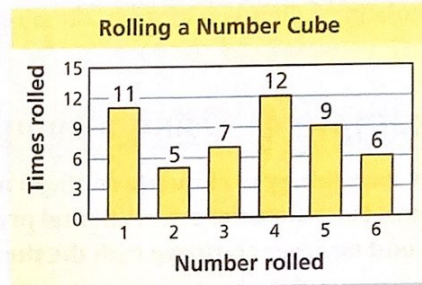
3. What is the theoretical probability of randomly choosing an X?

$$\frac{1}{7} = 0.1428$$

about 14%

Example 3 Comparing Probabilities

The bar graph shows the results of rolling a number cube 50 times. How does the experimental probability of rolling an odd number compare with the theoretical probability?



Step 1: Find the experimental probability of rolling an odd number.

The bar graph shows 11 ones, 7 threes, and 9 fives. So, an odd number was rolled $11 + 7 + 9 = 27$ times in a total of 50 rolls.

$$P(\text{odd}) = \frac{\text{number of times an odd number was rolled}}{\text{total number of rolls}}$$

$$= \frac{27}{50}, \text{ or } 54\%$$

experimental

$$11 + 7 + 9 = 27$$

$$\frac{27}{50} = 54\%$$

Step 2: Find the theoretical probability of rolling an odd number.

$$P(\text{odd}) = \frac{\text{number of favorable outcomes}}{\text{number of possible outcomes}} = \frac{3}{6} = \frac{1}{2}, \text{ or } 50\%$$

theoretical

How many odd #'s on a die?

$$\frac{3}{6} = 50\%$$

- The experimental probability of rolling an odd number is 54%, which is close to the theoretical probability of 50%.

Try It

4. In Example 3, how does the experimental probability of rolling a number greater than 1 compare with the theoretical probability?

experimental - How many times we rolled greater than 1

$$5 + 7 + 12 + 9 + 6 = \frac{39}{50 \text{ total}} = 78\%$$

theoretical - How many numbers are greater than 1 on a dice

2, 3, 4, 5, 6

$$\frac{5}{6} = \text{about } 83\%$$

They are close to each other.